

Topic Exam

Functions & Equations

Video Solutions to this exam can be found at:

www.revisionvillage.com/functions-equations-exam



Question 1

[Maximum mark: 6]



Let $f(x) = x^3$ and g(x) = 2x - 1.

(a) Find
$$g^{-1}(x)$$
. [2]

(b) Find
$$g \circ f(x)$$
. [2]

(c) Solve
$$g \circ f(x) = 0$$
. [2]



Question 2

[Maximum mark: 5]



Let $f(x) = a(x - h)^2 + k$. The vertex of the graph of f is at (3,4) and the graph passes through (1,-4).

(a) Write down the value of h and k. [2]

(b) Find the value of a. [3]



Question 3

[Maximum mark: 7]



Let
$$f(x) = x^2 - 4x + 3$$

- (a) For the graph of f, find
 - (i) y-intercept;
 - (ii) x-intercepts.

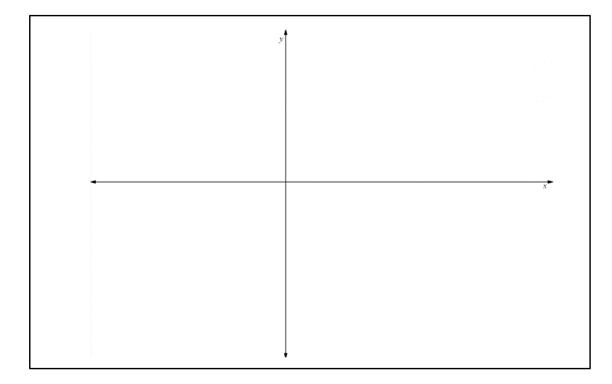
[3]

- (b) The function can also be expressed in the form $f(x) = (x h)^2 + k$.
 - (i) Find the value of h;
 - (ii) Find the value of k.

[2]

(c) Sketch the graph of *f* on the axis below. Clearly label the intercepts and vertex.

[2]





Question 4

[Maximum mark: 6]



Let
$$f(x) = \sqrt{x+7}$$
, for $x \ge -7$.

(a) Find
$$f^{-1}(3)$$
. [3]

(b) Let g be a function such that g^{-1} exists for all real numbers. Given that g(9)=4, find $(f\circ g^{-1})(4)$.



Question 5

[Maximum mark: 6]



Let $f(x) = (x+2)^3$ for $x \in \mathbb{R}$

(a) Find
$$f^{-1}(x)$$
 [3]

(b) Let g be a function so that $f \circ g(x) = 27x^6$. Find g(x). [3]



Question 6

[Maximum mark: 7]



Let $f(x) = x^2 + kx$ and g(x) = x + k. The graphs of f and g intersect at two distinct points.

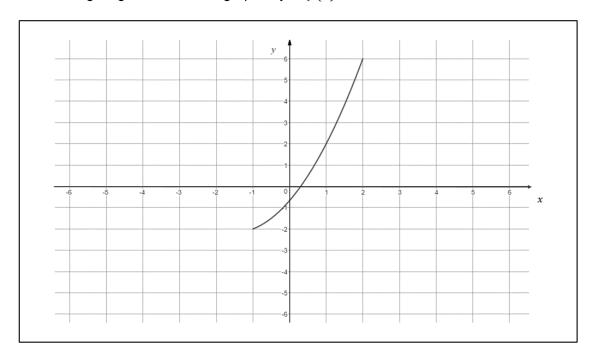
Find the values of k.

Question 7

[Maximum mark: 6]



The following diagram shows the graph of y = f(x).



(a) Write down the value of

(i) f(1);

(ii)
$$f^{-1}(-2)$$
. [2]

(b) Find $f \circ f(1)$. [2]

(c) Sketch the graph of y = f(-x) on the grid above. [2]

Question 8

[Maximum mark: 15]



Let $f(x) = 3x^2 + 12x + 9$

- (a) (i) Find the y-intercept of f;
 - (ii) Find the x-intercepts of f.

[4]

The function can be written in the form $f(x) = a(x - h)^2 + k$.

- (b) Find the value of
 - (i) a;
 - (ii) h;
 - (iii) k;

[5]

- (c) (i) Write down the co-ordinate of the vertex of f.
 - (ii) Write down the equation of the axis of symmetry of f.

[2]

(d) The function g(x) is obtained from the graph of f by a reflection in the x-axis, followed by a translation by the vector $\begin{bmatrix} 0 \\ 4 \end{bmatrix}$. Find g, giving your answer in the form $g(x) = Ax^2 + Bx + C$.

[4]

Question 9

[Maximum mark: 15]



Let
$$f(x) = \frac{5}{x+1}$$
 and $g(x) = x - 3$.

- (a) For the graph of f, find
 - (i) y-intercept;
 - (ii) x-intercept;
 - (iii) the equation of the vertical asymptote. [5]
- (b) The graph of f and g intersect at A(x,y) and point B(x,y). Find the coordinates of points A and B. [5]
- (c) Find the equation of the linear line that passes through A and B, in the form [3] of y = mx + c.
- (d) Write down the gradient of the line that is perpendicular to the line passing [2] through A and B.

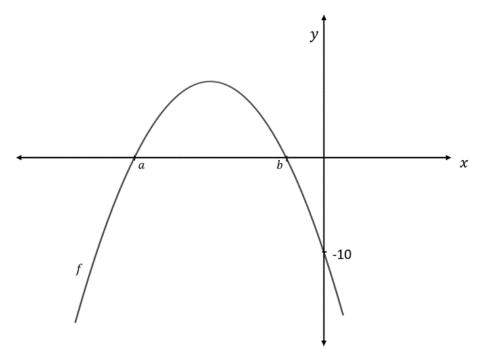


Question 10

[Maximum mark: 15]



Let f(x) = p(x+1)(x+5). The following diagram shows part of the graph of f.



The graph has x-intercepts at (a, 0) and (b, 0), and a y-intercept at (0, -10).

- (a) (i) Write down the value of a and of b.
 - (ii) Find the value of p.

[6]

(b) Find the equation of the axis of symmetry.

[2]

(c) Find the co-ordinate of the vertex.

[3]

[4]

(d) Point A(-2,6) lies on the curve of f. The graph of g is obtained from the graph of f by a reflection of f in the y-axis, followed by a translation by the vector $\begin{bmatrix} 0 \\ 2 \end{bmatrix}$. Point A is mapped to the point A' on the graph of g. Find A'